



Solving Equations

Knowledge Organiser

One unknown

Solve $2x + 3 = 9$

$$\begin{array}{rcl} -3 & -3 & \\ 2x & = & 6 \\ \div 2 & \div 2 & \\ x & = & 3 \end{array}$$

Solve $3x - 5 = 4$

$$\begin{array}{rcl} +4 & +4 & \\ 3x & = & 9 \\ \div 3 & \div 3 & \\ x & = & 3 \end{array}$$

Solve $3x + 2 = -7$

$$\begin{array}{rcl} -2 & -2 & \\ 3x & = & -9 \\ \div 3 & \div 3 & \\ x & = & -3 \end{array}$$

Solve $2(x + 1) = 9$

$$\begin{array}{rcl} 2x + 2 & = & 9 \\ -2 & -2 & \\ 2x & = & 7 \\ \div 2 & \div 2 & \\ x & = & 3.5 \end{array}$$

Find the area of the square



13

$3x + 4$

$$\begin{array}{rcl} 3x + 4 & = & 13 \\ -4 & -4 & \\ 3x & = & 9 \\ \div 3 & \div 3 & \\ x & = & 3 \end{array}$$

Two unknowns

Solve $2x + 1 = x + 9$

$$\begin{array}{rcl} -1 & -1 & \\ 2x & = & x + 8 \\ -x & -x & \\ x & = & 8 \end{array}$$

Solve $2x - 2 = x + 4$

$$\begin{array}{rcl} +2 & +2 & \\ 2x & = & x + 6 \\ -x & -x & \\ x & = & 6 \end{array}$$

Solve $2x + 4 = x - 7$

$$\begin{array}{rcl} -4 & -4 & \\ 2x & = & x + 11 \\ -x & -x & \\ x & = & 11 \end{array}$$

Solve $4x + 1 = x + 10$

$$\begin{array}{rcl} -1 & -1 & \\ 4x & = & x + 9 \\ -x & -x & \\ 3x & = & 9 \\ x & = & 3 \end{array}$$

Find the area of the square



$2x + 4$

$x + 8$

$2x + 4 = x + 8$

$$\begin{array}{rcl} -4 & -4 & \\ 2x & = & x + 4 \\ -x & -x & \\ x & = & 4 \end{array}$$

If $x = 4$ then
 $2 \times 4 + 4 = 12$
 And
 $4 + 8 = 12$

Answer =
 $12 \times 12 = 144$



Setting up equations & simultaneous equations

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Key Words

equation

solve

simultaneous

Solving Equations

Solve $2x + 1 = 7$

$$\begin{array}{r} -1 \quad -1 \\ 2x = 6 \\ \div 2 \quad \div 2 \\ x = 3 \end{array}$$

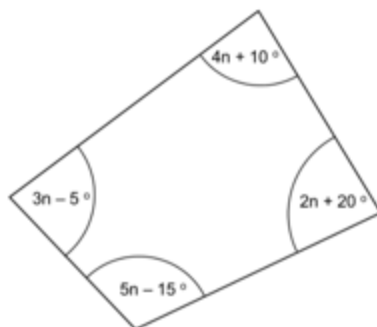
Solve $2x + 3 = x + 6$

$$\begin{array}{r} -3 \quad -3 \\ 2x = x + 3 \\ -x \quad -x \\ x = 3 \end{array}$$

Solve $3x - 2 = x + 6$

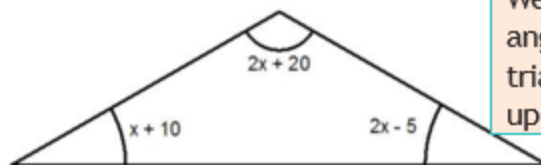
$$\begin{array}{r} +2 \quad +2 \\ 3x = x + 8 \\ -x \quad -x \\ 2x = 8 \\ \div 2 \quad \div 2 \\ x = 4 \end{array}$$

Setting up and solving equations

Find the value of n 

We know that angles in quadrilaterals add up to 360°

$$\begin{aligned} 3n - 5 + 5n - 15 + 4n + 10 + 2n + 20 &= 360 \\ 14n + 10 &= 360 \\ 14n &= 350 \\ n &= 25^\circ \end{aligned}$$

Find the value of x 

We know that angles in triangles add up to 180°

$$\begin{aligned} x + 10 + 2x + 20 + 2x - 5 &= 180 \\ 5x + 25 &= 180 \\ 5x &= 155 \\ x &= 31^\circ \end{aligned}$$

Simultaneous Equations

Remember STOP

Same-sign, take away, opposite-sign, plus

$$\begin{array}{r} 1) \quad 6x + y = 26 \\ + \quad 2x - y = 6 \\ \hline 8x = 32 \\ x = 4 \\ \text{Substitute in } x = 4 \\ 8 - y = 6 \\ y = 2 \end{array}$$

$$\begin{array}{r} 2) \quad 6x + y = 27 \\ - \quad 4x + y = 11 \\ \hline 2x = 16 \\ x = 8 \\ \text{Substitute in } x = 8 \\ 32 + y = 11 \\ y = -21 \end{array}$$

Problem Solving

A lamp and a bulb together cost £32.

The lamp costs £30 more than the bulb.

How much does the bulb cost?



Let the lamp = L
Let the bulb = B

$$L + B = 32$$

$$B + 30 = L$$

$$(B + 30) + B = 32$$

$$2B + 30 = 32$$

$$2B = 2$$

$$B = 1$$

$$\text{If } B = 1 \text{ then } L + 1 = 32$$

$$\text{So } L = 31$$



Expanding & Factorising

Key Words

Expanding

Factorising

Expanding & Factorising Single Brackets

Expand $2(x + 1)$

$$= 2x + 2$$

Expand $3(2x - 4)$

$$= 6x - 12$$

Expand $4x(2x - 5)$

$$= 8x^2 - 20x$$

Factorise $6x + 12$

$$= 6(x + 2)$$

Factorise $x^2 + 3x$

$$= x(x + 3)$$

Factorise $30x + 40$

$$= 10(3x + 4)$$

Expanding Double Brackets

$$(x+2)(x+3)$$

$$\begin{aligned} & (x+2)(x+3) \\ & = x^2 + 3x + 2x + 6 \\ & = x^2 + 5x + 6 \end{aligned}$$

$$(x+5)(x-7)$$

$$\begin{aligned} & (x+5)(x-7) \\ & = x^2 - 7x + 5x - 35 \\ & = x^2 - 2x - 35 \end{aligned}$$

$$(x+4)^2$$

$$\begin{aligned} & (x+4)^2 \\ & = (x+4)(x+4) \\ & = x^2 + 4x + 4x + 16 \\ & = x^2 + 8x + 16 \end{aligned}$$

$$(x-7)(x-3)$$

$$\begin{aligned} & (x-7)(x-3) \\ & = x^2 - 3x - 7x + 21 \\ & = x^2 - 10x + 21 \end{aligned}$$

Find the area



$x - 2$

$$4x + 3$$

To find the area of a rectangle we need to multiply

$$(4x+3)(x-2)$$

$$\begin{aligned} & (4x+3)(x-2) \\ & = 4x^2 - 8x + 3x - 6 \\ & = 4x^2 - 5x - 6 \end{aligned}$$

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Factorising Double Brackets

Factorise $x^2 + 7x + 10$

We need to find two numbers that multiply to give 10 and add to give 7. List the factors of 10:

$$1 \times 10$$

$$5 \times 2 \dots (5 + 2 = 7)$$

$$\text{Answer} = (x + 2)(x + 5)$$

Factorise $x^2 + 2x - 8$

We need to find two numbers that multiply to give -8 and add to give 2. List the factors of -8:

$$1 \times -8$$

$$-1 \times 8$$

$$2 \times -4$$

$$4 \times -2 \dots (4 + -2 = 2)$$

$$\text{Answer} = (x + 4)(x - 2)$$



Ratio

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Key Words

Simplify

Share

Ratio

Ratio & Fractions

Write 1:3 as fractions

There are 4 parts altogether:

$$\frac{1}{4} : \frac{3}{4}$$

Write 2:6 as fractions

There are 8 parts altogether:

$$\frac{2}{8} : \frac{6}{8}$$

Simplifying Ratio

Simplify 6: 12

$$\div 6 \quad \div 6$$

$$1:2$$

Simplify 3: 15

$$\div 3 \quad \div 3$$

$$1:2$$

Simplify 10: 20

$$\div 2 \quad \div 2$$

$$1:2$$

Simplify 12: 18

$$\div 6 \quad \div 6$$

$$2:3$$

Simplify 18: 27

$$\div 9 \quad \div 9$$

$$2:3$$

Simplify 32: 48

$$\div 8 \quad \div 8$$

$$4:6$$

'More than' Questions

Sarah and Jim share some money in the ratio 2:4. Jim gets £10 more than Sarah. How much does Sarah get?

Jim gets 2 parts and £10 more.

2 parts = £10

1 part = £5

So Sarah = $2 \times £5 = £10$

Sharing Ratio

Split £20 into the ratio 2:3

$$2 + 3 = 5$$

$$20 \div 5 = 4 \text{ (1 part)}$$

$$2 \times 4: 3 \times 4$$

$$8: 12$$

Split £100 into the ratio 5:7:8

$$5 + 7 + 8 = 20$$

$$100 \div 20 = 5 \text{ (1 part)}$$

$$5 \times 5 : 7 \times 5: 8 \times 5$$

$$25:35:40$$

Sarah and Jim share some money in the ratio 1:5. Jim gets £20 more than Sarah. How much does Sarah get?

Jim gets 4 parts and £20 more.

4 parts = £20

1 part = £5

So Sarah = $1 \times £5 = £5$